

Decoherence of charge qubit coupled to interacting background charges

Igor V. Yurkevich,^{1,2} Jim Baldwin,¹ Igor V. Lerner,^{1,3} and Boris L. Altshuler^{4,3}

¹*School of Physics and Astronomy, University of Birmingham, Birmingham B15 2TT, United Kingdom*

²*Institut für Nanotechnologie, Forschungszentrum Karlsruhe, 76021 Karlsruhe, Germany*

³*Institute for Nuclear Theory, University of Washington, Seattle, WA 98195, USA*

⁴*Physics Department, Columbia University, 538 West 120th Street, New York, N.Y. 10027, USA*

The major contribution to decoherence of a double quantum dot or a Josephson junction charge qubit comes from the electrostatic coupling to fluctuating background charges hybridized with the conduction electrons in the reservoir. However, estimations according to previously developed theories show that finding a sufficient number of effective fluctuators in a realistic experimental layout is quite improbable. We show that this paradox is resolved by allowing for a short-range Coulomb interaction of the fluctuators with the electrons in the reservoir. This dramatically enhances both the number of effective fluctuators and their contribution to decoherence, resulting in the most dangerous decoherence mechanism for charge qubits.

PACS numbers: 03.65.Yz, 73.23.Hk, 85.25.Cp

An implementation of quantum logical gates using solid-state nano-devices looks rather desirable due to their potential scalability. One of possible routes in this direction is developing of charge qubits. Schematically, a charge qubit is a contact of two normal or superconducting islands with charge carriers tunneling between them. The gate-controlled Coulomb blockade separates two charge states from all the others thus making a qubit [1, 2, 3]. Experimentally such charge qubits have been built as double quantum dots (DQD) [4, 5, 6, 7] or Josephson junction structures, made of a small superconducting island connected via a Josephson junction to superconducting reservoirs [8, 9, 10, 11, 12, 13].

Decoherence due to coupling to the environment remains a major impediment for developing charge qubits. This determines the demand for a better theoretical understanding of the microscopic mechanisms that lead to decoherence. It is widely believed that the main contribution to decoherence in charge qubits comes from its coupling to fluctuating background charges (FBCs) that create dynamical electric field, which affects qubit charge states (see ref. [14] for reviews of experimental evidence). Since charge impurities are spatially quenched in the experimental temperature range $T \sim 20 \div 50$ mK, the most probable cause for FBCs is from random recharging of electron traps embedded in an insulating layer close to the electronic bath. The role of the bath can be played by normal as well as superconducting metallic leads or gates when the electron states on the traps are hybridized with those in the bath. The appropriate model for FBCs has been developed [15, 16, 17, 18, 19, 20, 21, 22, 23] by analogy with the spin-fluctuator model of the spectral diffusion in glasses [24]. In its frame, relevant experimental findings on the decoherence and dephasing in charge qubits have been successfully explained [25].

The question which has not yet been addressed is whether there is enough of FBCs to cause experimentally observed decoherence. For a typical DQD qubit, the

area of the electrodes is of order of μm^2 and the volume available for the FBCs which can contribute to decoherence can be estimated as $10^{-15} \div 10^{-16} cm^3$ so that their number is $N_{\text{geom}} \sim (10 \div 100)c$ where c is their number concentration measured in ppm (parts per million).

As the appropriate electronic levels are randomly spread in the energy interval of the order of the bandwidth, $D \sim 1 \div 10$ eV, the effective number of traps N_{eff} is reduced in comparison to N_{geom} by a factor of δ/D where δ is the interval of energies in which FBCs are effective. Classical considerations [15, 16, 17] suggest that δ is of the order of the relevant temperature, $T \sim 10 \div 50 \mu K$, while the electronic trap levels separated from the Fermi sea by energies $\varepsilon_0 \gtrsim T$ are frozen out, i.e. their contribution is exponentially suppressed. Had this been the case, N_{eff} would be five orders in magnitude below N_{geom} . Then the probability to find even a single effective FBC would be negligible for any realistic value of c .

The full quantum considerations [18, 23] show that electron traps energy levels up to $\varepsilon_0 \lesssim \gamma_0$, contribute to decoherence. Here γ_0 is the hybridization energy, i.e. the broadening of the appropriate level. Its typical value can be much higher than T but still is likely to be much smaller than D . The effective number of traps is thus

$$N_{\text{eff}} \sim \frac{\gamma_0}{D} N_{\text{geom}}. \quad (1)$$

Even with this enhancement N_{eff} still seems to be of order 1 or even smaller for cleaner samples, with $c \sim 1$ ppm. At the same time experiments [8-13] show that even the cleanest samples suffer from considerable decoherence. Moreover, assuming that FBCs, indeed, limit the decoherence and relaxation, one can explain [16] experimentally observed [13] $1/f$ noise only *provided that* the number of FBCs is large. Thus it looks that the above considerations underestimate the efficiency of this source of decoherence.

In this letter we show that allowing for the Coulomb interaction between the trapped charge and bath elec-

trons results in a dramatic increase of the effective hybridization rate γ and thus in the upward revision of the estimate (1). We will present full analytic results that show how the interaction enhances decoherence.

We consider the model [15, 16] of the charge qubit indirectly coupled to the thermal bath via the coupling $\hat{V} = \sum_{i,\sigma} v_i \hat{d}_{i\sigma}^\dagger \hat{d}_{i\sigma}$ to FBCs hybridized with the bath:

$$\hat{H}_Q = \left(\frac{\omega_0}{2} - \hat{V}\right) \hat{\tau}_z - \frac{E}{2} \hat{\tau}_x + \hat{H}_B. \quad (2)$$

Here $\omega_0 = E_c(N - N_g)$ is the energy gap between the qubit levels, $\hat{\tau}_i$ are the Pauli matrices in the space of qubit states, E is the control energy (that includes the Josephson energy in case of the JCQ); $\hat{d}_{i\sigma}^\dagger, \hat{d}_{i\sigma}$ are the creation and annihilation operators for an electron with spin $\sigma = \uparrow, \downarrow$ at the i^{th} trap and v_i is the electrostatic coupling of the qubit to the trapped electron.

We assume that the bath, described by H_B , is a normal metal – the situation which is more relevant for the DQD charge qubit (for the JCQ this mechanism might be relevant as well since in the absence of screening spatially remote trapped electrons hybridized with metallic gates may contribute to decoherence). In this case

$$\hat{H}_B = \hat{H}_{\text{met}} + \hat{H}_{\text{imp}} + \hat{H}_{\text{int}}. \quad (3)$$

Here $\hat{H}_{\text{met}} = \sum_{\mathbf{p},\sigma} \varepsilon_{\mathbf{p}} \hat{c}_{\mathbf{p},\sigma}^\dagger \hat{c}_{\mathbf{p},\sigma}$ is the Hamiltonian of the metallic bath, $\hat{c}_{\mathbf{p},\sigma}^\dagger, \hat{c}_{\mathbf{p},\sigma}$ creation and annihilation operators for bath electrons. The energy $\varepsilon_{\mathbf{p}} \equiv p^2/2m - \varepsilon_F$ is counted from the chemical potential (and so are ε_i below). The impurity Hamiltonian describes random levels which can trap electrons,

$$\hat{H}_{\text{imp}} = \sum_i [\varepsilon_i \hat{n}_i + U_i^H \hat{n}_{i\uparrow} \hat{n}_{i\downarrow}], \quad (4)$$

where $\hat{n}_{i\sigma} = \hat{d}_{i\sigma}^\dagger \hat{d}_{i\sigma}$ and $\hat{n}_i = \hat{n}_{i\uparrow} + \hat{n}_{i\downarrow}$. The Hubbard on-site repulsion U_i^H is assumed to be very large so that two electrons cannot reside on the same site. The relevant charge fluctuations are due to switchings between empty and single-occupied impurity states. In what follows we disregard double-occupied states and omit irrelevant spin indices, absorbing the spin degeneracy of the bulk electrons into the density of states $\nu_0 \equiv 1/\mathcal{V}\delta$.

The d -electrons are coupled to the bath via direct hybridization as well as via the local Coulomb interaction:

$$\hat{H}_{\text{int}} = \sum_{i,\mathbf{p}} [t_i \hat{c}_{\mathbf{p}}^\dagger \hat{d}_i + \text{h.c.}] + \sum_i U_i \hat{n}_i \hat{\rho}_i. \quad (5)$$

Here t_i is the tunneling amplitude from the resonant level at the i^{th} trap into the bulk, $\hat{\rho}_i$ is the bath electron density operator at the i^{th} site and the interaction U_i is positive for an acceptor and negative for a donor level.

The model of Eqs. (2)–(5) was previously considered [15, 16, 17, 18, 19, 20, 21, 22, 23] without the interactions U_i in Eq. (5). We will extend the non-perturbative

procedure developed in [18] to evaluate the contribution to decoherence of the charge qubit due to FBCs interacting with the bath electrons.

Let the full density matrix of the system initially be separable, i.e. $\hat{\rho}_{B+Q}(0) = \hat{\rho}(0) \otimes \hat{\rho}_B$, where $\hat{\rho}(t)$ is the reduced density matrix of the qubit and $\hat{\rho}_B = Z_B^{-1} e^{-\beta \hat{H}_B}$ is the equilibrium density matrix of the bath. Then one can formally represent $\hat{\rho}(t)$ as

$$\hat{\rho}(t) = \begin{pmatrix} n(t) & \rho_{12}(0) e^{-i\omega_0 t} \mathcal{D}(t) \\ \rho_{21}(0) e^{i\omega_0 t} \mathcal{D}^*(t) & 1 - n(t) \end{pmatrix}. \quad (6)$$

In the long-time limit, both diagonal and off-diagonal elements of $\hat{\rho}(t)$ get exponentially close to their equilibrium values. The corresponding decay rates are usually referred to as the relaxation, Γ_1 , and decoherence, Γ_2 , rates. Below we discuss “pure dephasing”, i.e. let $E = 0$ in Eq. (2). This is justified for the charge qubit during the most of the operational cycle [15]. We find the time evolution of $\mathcal{D}(t)$ as

$$\mathcal{D}(t) = \left\langle e^{i(\hat{H}_B + \hat{V})t} e^{-i(\hat{H}_B - \hat{V})t} \right\rangle \quad (7)$$

where $\langle \hat{A} \rangle \equiv \text{Tr}(\rho_B \hat{A})$. As $\Gamma_2 = -\lim_{t \rightarrow \infty} t^{-1} \ln |D(t)|$, we need to calculate the asymptotical value of $\mathcal{D}(t)$ at $t \rightarrow \infty$. To this end, we represent $\mathcal{D}(t)$ in Eq. (7) as a functional integral over the Keldysh double-time contour, which is natural as Eq. (7) contains time-ordered and anti-time-ordered exponentials.

Note now that Eqs. (3)–(5) determine a well known problem of the interacting resonant level (IRL) which can be mapped [26] onto the single channel Kondo problem. This suggests that one can account for the interaction (the second term in Eq. (5)) by using the renormalization group approach. We will show that this leads only to substituting the renormalized (energy-dependent) hybridization rate for the bare one into Eq. (11a) below.

In the absence of the interaction term in Eq. (5) one performs an exact functional integration over the fields describing electrons in the bath. This results in the effective action in terms of the fields $\hat{d}_i(t), d_i(t)$ which describe trapped electrons

$$\mathcal{S}[d^\dagger, d] = \sum_{ij} \int dt dt' d_i^\dagger(t) \hat{G}_{ij}^{-1}(t, t') d_j(t'). \quad (8)$$

The time integrations are performed along the standard Keldysh contours. The Keldysh Green function $\hat{G}_{ij}(t, t')$ of the FBC is defined by the Dyson equation resulted from the integration over the bath electron fields:

$$\begin{aligned} \hat{G}_{ij}^{-1}(t, t') &= \delta(t, t') \delta_{ij} [i\partial_t - \varepsilon_i + v_i(t, t')] - \hat{\Sigma}_{ij}(t, t'), \\ \hat{\Sigma}_{ij}(t, t') &= t_i t_j^* \hat{g}(\mathbf{r}_i - \mathbf{r}_j; t - t'). \end{aligned} \quad (9)$$

Here $v_i(t, t') = \pm \theta(t) \theta(t - t') v_i$ with ‘+’ sign on the upper and ‘−’ sign on the lower branch of the Keldysh contour,

and \hat{g} is the bare Keldysh Green function of the conduction electrons: the Fourier transforms of its retarded component is $g^R(\varepsilon, \mathbf{p}) = (\varepsilon - \varepsilon_{\mathbf{p}} + i0)^{-1}$. Typically, FBCs are separated by a distance far exceeding λ_F . Then the off-diagonal contributions to Σ_{ij} is suppressed upon a spatial integration. Thus $\hat{G}_{ij} = \hat{G}_i \delta_{ij}$ with $G_i^R(\varepsilon) = (\varepsilon - \varepsilon_i + i\gamma_i/2)^{-1}$ and $G_i^K(\varepsilon) = 2 \text{Im} G_i^R(\varepsilon) \tanh(\varepsilon/2T)$. The width $\gamma_i = \text{Re} \Sigma_{ii} = \pi |t_i|^2 / \delta$ of the i^{th} trap level plays the role of the recharging switching rate.

Since contributions of different FBCs are uncorrelated, we consider a single fluctuator with the switching rate γ_0 . Then the functional averaging in Eq. (7) with the action (8) results in

$$\Gamma_2 = -\text{Re} \lim_{t \rightarrow \infty} t^{-1} \text{Tr} \ln(1 + \hat{v} \hat{G}).$$

After expanding this in powers of $\hat{v} \hat{G}$, one finds that the t^{-1} factor cancels while the remaining time-integrals in each order have the convolution structure [18]. This allows to re-exponentiate the expansion after performing the Fourier transform. Taking then the trace in the Keldysh space, we arrive at

$$\Gamma_2 = -\Re \int_{-\infty}^{+\infty} \frac{d\varepsilon}{2\pi} \ln [1 + v G^K(\varepsilon) - v G^R(\varepsilon) v G^A(\varepsilon)]. \quad (10)$$

Substituting $G^{R,A}$ and G^K into Eq. (10) we find Γ_2 as a function of T and $\gamma(\varepsilon)$:

$$\Gamma_2 = - \int_{-\infty}^{\infty} \frac{d\varepsilon}{4\pi} \ln \{1 - 4f(\varepsilon)[1 - f(\varepsilon)] \sin^2 \varphi(\varepsilon)\}, \quad (11a)$$

where $f(\varepsilon) \equiv (1 + e^{\varepsilon/T})^{-1}$ is the Fermi factor and

$$\varphi(\varepsilon) = \arctan \frac{2v\gamma(\varepsilon)}{(\varepsilon - \varepsilon_0)^2 + \gamma^2(\varepsilon) - v^2}. \quad (11b)$$

Note that the interaction in Eq. (5) entered Γ_2 only through substituting the renormalized energy-dependent switching rate $\gamma(\varepsilon)$ for the bare value γ_0 . The RG equations for the IRL model, Eqs. (3)–(5), have been obtained by mapping the tunneling amplitude t_0 onto the transverse coupling J_{\perp} in the Kondo model (see, e.g., [27, 28, 29]). These RG equations are equivalent to those originally derived for the Kondo model within the 1D Coulomb gas picture [30]. It is convenient to write them in terms of the effective charges Y and δ ,

$$\frac{dY}{d \ln \epsilon} = \left[-1 - 2\frac{\delta}{\pi} + \left(\frac{\delta}{\pi}\right)^2 \right] Y, \quad \frac{d\delta}{d \ln \epsilon} = \left(1 - \frac{\delta}{\pi} \right) Y^2,$$

where $\delta \equiv 2 \arctan(\pi \nu_0 U/2)$, $Y \equiv (\gamma/\epsilon) \cos^2 \delta$ and ϵ is the running energy cutoff. The upper cutoff is the bandwidth D of the bath electrons. As typically $\gamma_0 \ll D$, the bare value $Y_0 \sim \gamma_0/D \ll 1$ so that one can neglect the

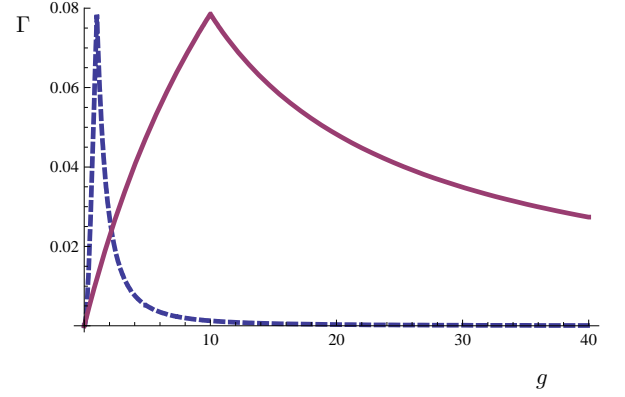


FIG. 1: Decoherence rate as a function of coupling strength, $g \equiv v/\gamma$, for $T = 0.1\gamma$, $D = 10\gamma$. The dashed line shows the non-interacting case ($\alpha = 0$), while the solid line describes decoherence with allowance for the interaction ($\alpha = 0.5$) which turns out to be substantial in a much wider parametric range.

renormalization of δ . Substituting $\delta = \delta_0$, we rewrite the RG equations as

$$\frac{d \ln \gamma}{d \ln \epsilon} = -\alpha, \quad \alpha \equiv 2 \frac{\delta_0}{\pi} - \left(\frac{\delta_0}{\pi} \right)^2. \quad (12)$$

Equation (12) yields $\gamma(\varepsilon) = \gamma_0 (D/\varepsilon)^\alpha$. The energy dependence saturates for small ε at $\varepsilon = \max(\gamma, T, \varepsilon_0)$. The parameter α can be positive or negative, depending on the interaction sign. For $U_0 > 0$ the linear in δ contribution to α (due to the Mahan exciton) is dominant [31] and exceeds the quadratic contribution (due to the Anderson orthogonality catastrophe) so that $\alpha > 0$. Below we take into account only the levels with positive α .

According to Eq. (11) all traps with $\gamma(\varepsilon) > \varepsilon_0$ contribute effectively to Γ_2 . Since $\gamma(\varepsilon) \gg \gamma_0$ for $\alpha > 0$, the fraction of effective FBCs dramatically increases in comparison to the non-interacting case.

At a given T each FBC is either in the high-temperature, $T \gtrsim \gamma(\varepsilon)$, or in the low-temperature, $T \lesssim \gamma(\varepsilon)$, regime, depending on the relation between T and $T_0 \equiv \gamma_0 (D/\gamma_0)^{\frac{\alpha}{1+\alpha}}$. As $\varepsilon_0 \lesssim \gamma_0$ the effective number, Eq. (1), of “high- T ” FBCs can be estimated as $(T/D)^{1+\alpha} N_{\text{geom}}$, making their presence rather improbable – but not impossible. The switching rate for such FBCs is T -dependent and saturated at $\gamma(T) = \gamma_0 (D/T)^\alpha$. Most (if not all) FBCs are in the low- T regime, $T \lesssim \gamma(\varepsilon)$, i.e. characterized by T_0 exceeding T . In this case the switching rate $\gamma(\varepsilon)$ saturates at $\gamma = \gamma_0 (D/\gamma)^{\alpha/(1+\alpha)}$.

Since at low T the product of Fermi factors in Eq. (11a) is a peak around zero (i.e. the Fermi energy) of width T , we approximate $\gamma(\varepsilon)$ by the ε -independent expression,

$$\gamma \approx \gamma(\varepsilon = \gamma_0) = \begin{cases} \gamma_0 (D/\gamma_0)^{\frac{\alpha}{1+\alpha}}, & \gamma \gtrsim \varepsilon_0 \\ \gamma_0 (D/\varepsilon_0)^\alpha, & \gamma \lesssim \varepsilon_0 \end{cases} \quad (13)$$

Thus the contribution of the low- T FBC into the decoherence rate is

$$\Gamma_2^{\text{low}}(T) = \frac{T}{\pi} \arctan^2 \left[\frac{2v\gamma}{\varepsilon_0^2 + \gamma^2 - v^2} \right]. \quad (14)$$

Figure 1 illustrates this behavior and shows that the interaction dramatically increases the energy where FBCs effectively contribute to Γ_2 . For $\varepsilon_0 \gg \gamma$ the decoherence rate decays with ε_0 faster than in the non-interacting case: $\Gamma_2 \propto \varepsilon_0^{-4-2\alpha}$. This means that, as was noticed above, only FBCs with $\varepsilon_0 \lesssim \gamma$ cause decoherence. Using γ from the upper line in Eq. (13) we find the effective number of FBCs:

$$N_{\text{eff}} \sim \left(\frac{\gamma_0}{D} \right)^{\frac{1}{1+\alpha}} N_{\text{geom}}. \quad (15)$$

This is considerably higher than that in the absence of the interaction, Eq. (1).

We have already noticed that it is statistically improbable to find the FBCs in the high- T regime. Had they existed, their contribution would be also enhanced by the interaction as compared to the expressions obtained classically [15, 16], namely

$$\Gamma_2^{\text{high}}(T) = \gamma(T) - \theta(\gamma(T) - v) \sqrt{\gamma^2(T) - v^2}, \quad (16)$$

where $\gamma(T) = \gamma_0 (D/T)^\alpha$. Eq. (16) predicts a non-analytic in T decoherence rate with a well pronounced peak at $T = Dg^{-1/\alpha}$.

In conclusion, we have demonstrated that the fluctuating background charges – namely, electrons trapped in the insulating layer close to the surface of metallic gates/electrodes and thus hybridized and interacting with the conduction electrons – cause significant decoherence of the charge qubit. The interaction leads to a drastic increase of the efficiency of this mechanism of decoherence and to a parametric enhancement of the resulting contribution, as well as of the number of the effective FBCs given by Eq. (15). This enhancement proves the assumption that the FBCs act as the most dangerous source of decoherence for the charge qubit.

We thank Yuri Galperin for useful discussions. This work was supported by the EPSRC grant T23725/01 and by the US DOE contract No. DE-AC02-06CH11357.

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- [1] A. Shnirman, G. Schön, and Z. Hermon, *Phys. Rev. Lett.* **79**, 2371 (1997); Y. Makhlin, G. Schön, and A. Shnirman *Nature* **398**, 305 (1999).
 - [2] F. Plastina and G. Falci, *Phys. Rev. B* **67**, 224514 (2003).
 - [3] D. V. Averin and C. Bruder, *Phys. Rev. Lett.* **91**, 057003 (2003).
 - [4] T. Hayashi, T. Fujisawa, H. D. Cheong, Y. H. Jeong, and Y. Hirayama, *Phys. Rev. Lett.* **91**, 226804 (2003).

- [5] J. R. Petta, A. C. Johnson, C. M. Marcus, M. P. Hanson, and A. C. Gossard, *Phys. Rev. Lett.* **93**, 186802 (2004).
- [6] J. Gorman, D. G. Hasko, and D. A. Williams, *Phys. Rev. Lett.* **95**, 090502 (2005).
- [7] S. E. S. Andresen, R. Brenner, C. J. Wellard, C. Yang, T. Hopf, C. C. Escott, R. G. Clark, A. S. Dzurak, D. N. Jamieson, and L. C. L. Hollenberg, *Nano Lett.* **7**, 2000 (2007).
- [8] Y. Nakamura, Y. A. Pashkin, and J.S.Tsai, *Nature* **398**, 786 (1999).
- [9] D. Vion, A. Aassime, A. Cottet, P. Joyez, H. Pothier, C. Urbina, D. Esteve, and M. H. Devoret, *Science* **296**, 886 (2002).
- [10] Y. Yu, S. Han, X. Chu, S.-I. Chu, and Z. Wang, *Science* **296**, 889 (2002).
- [11] Y. A. Pashkin, T. Yamamoto, O. Astafiev, Y. Nakamura, D. V. Averin, and J. S. Tsai, *Nature* **421**, 823 (2003).
- [12] T. Duty, D. Gunnarsson, K. Bladh, and P. Delsing, *Phys. Rev. B* **69**, 140503(R) (2004).
- [13] O. Astafiev, Y. A. Pashkin, Y. Nakamura, T. Yamamoto, and J. S. Tsai, *Phys. Rev. Lett.* **96**, 137001 (2006).
- [14] Y. A. Pashkin, O. Astafiev, T. Yamamoto, Y. Nakamura, and J. S. Tsai, *Quantum Inf. Process.* **8**, 55 (2009).
- [15] E. Paladino, L. Faoro, G. Falci, and R. Fazio, *Phys. Rev. Lett.* **88**, 228304 (2002).
- [16] Y. M. Galperin, B. L. Altshuler, and D. V. Shantsev, *Low frequency noise as a source of dephasing of a qubit*, cond-mat/0312490.
- [17] L. Faoro, J. Bergli, B. L. Altshuler, and Y. M. Galperin, *Phys. Rev. Lett.* **95**, 046805 (2005).
- [18] A. Grishin, I. V. Yurkevich, and I. V. Lerner, *Phys. Rev. B* **72**, 060509(R) (2005).
- [19] R. de Sousa, K. B. Whaley, F. K. Wilhelm, and J. von Delft, *Phys. Rev. Lett.* **95**, 247006 (2005).
- [20] Y. M. Galperin, B. L. Altshuler, J. Bergli, and D. V. Shantsev, *Phys. Rev. Lett.* **96**, 097009 (2006).
- [21] S. Montangero, T. Calarco, and R. Fazio, *Phys. Rev. Lett.* **99**, 170501 (2007).
- [22] E. Paladino, M. Sassetti, G. Falci, and U. Weiss, *Phys. Rev. B* **77**, 041303(R) (2008).
- [23] B. Abel and F. Marquardt, *Phys. Rev. B* **78**, 201302(R) (2008).
- [24] J. R. Klauder and P. W. Anderson, *Phys. Rev.* **125**, 912 (1962).
- [25] The most probable alternative microscopic mechanism of decoherence, via the qubit coupling to the phonon bath, is not efficient for the charge qubit, provided that one chooses a realistic phonon spectra [32].
- [26] G. Toulouse, *Phys. Rev. B* **2**, 270 (1970).
- [27] P. Schlottmann, *Phys. Rev. B* **22**, 613 (1980).
- [28] K. A. Matveev and A. I. Larkin, *Phys. Rev. B* **46**, 15337 (1992).
- [29] L. Borda, K. Vladar, and A. Zawadowski, *Phys. Rev. B* **75**, 125107 (2007).
- [30] G. Yuval and P. W. Anderson, *Phys. Rev. B* **1**, 1522 (1970).
- [31] G. D. Mahan, *Many-particle Physics*, Springer (2000).
- [32] S. Vorojtsov, E. R. Mucciolo, and H. U. Baranger, *Phys. Rev. B* **71**, 205322 (2005); M. Thorwart, J. Eckel, and E. R. Mucciolo, *Phys. Rev. B* **72**, 235320 (2005).